

Tennessee Comprehensive Assessment Program

# TCAP/CRA 2013



3

## Task 1 Scoring Guide Multiplication Task

## 1. Multiplication Task Scoring Guide

### The CCSS for Mathematical Content (2 points)

3.OA.A.1 Indicates an understanding of multiplication expression  $x \times y$  as  $x$  equal groups of  $y$  objects using a diagram or an explanation. \_\_\_\_\_

(1 Point)

3.OA.B.5 Represents a diagram or an equation that shows one or both factors partitioned but with the same product as the original expression. Student may show: \_\_\_\_\_

- $7 \times 19 = (10 \times 7) + (9 \times 7)$
- $7 \times 19 = (7 \times 10) + (7 \times 9)$
- $7 \times 19 = (2 \times 19) + (2 \times 19) + (2 \times 19) + 19$
- $7 \times 19 = (7 \times 20) - (7 \times 1)$

(1 Point)

Total Content Points \_\_\_\_\_

### The CCSS for Mathematical Practice (2 points)

MP3 Communicates the relationship between the factors or products in  $(3 \times 9) + (3 \times 9)$  and in  $3 \times 18$ . Student may indicate that: \_\_\_\_\_

- 9 items plus 9 items is equal to 18 items in  $3 \times 18$ .
- the products of  $(3 \times 9) + (3 \times 9)$  and  $(3 \times 18)$  are equal.
- 9 groups and 9 groups make a total of 18 groups that each have 3 items.

(1 Point)

(MP3: Construct viable arguments and critique the reasoning of others.)

MP4 Represents with diagrams or equations the student's expression for solving  $7 \times 19$  and Dylan's expression or  $3 \times 18$ . \_\_\_\_\_

(1 Point)

(MP4: Model with mathematics.)

Total Practice Points \_\_\_\_\_

Total Awarded Points \_\_\_\_\_

## The CCSS for Mathematical Content Addressed in This Task

### Represent and solve problems involving multiplication and division.

3.OA.A.1 Interpret products of whole numbers, e.g., interpret  $5 \times 7$  as the total number of objects in 5 groups of 7 objects each. *For example, describe a context in which a total number of objects can be expressed as  $5 \times 7$ .*

### Understand properties of multiplication and the relationship between multiplication and division.

3.OA.B.5 Apply properties of operations as strategies to multiply and divide. *Examples: If  $6 \times 4 = 24$  is known, then  $4 \times 6 = 24$  is also known. (Commutative property of multiplication.)  $3 \times 5 \times 2$  can be found by  $3 \times 5 = 15$ , then  $15 \times 2 = 30$ , or by  $5 \times 2 = 10$ , then  $3 \times 10 = 30$ . (Associative property of multiplication.) Knowing that  $8 \times 5 = 40$  and  $8 \times 2 = 16$ , one can find  $8 \times 7$  as  $8 \times (5 + 2) = (8 \times 5) + (8 \times 2) = 40 + 16 = 56$ . (Distributive property.)*

## The CCSS for Mathematical Practice\*

1. Make sense of problems and persevere in solving them.
2. Reason abstractly and quantitatively.
3. Construct viable arguments and critique the reasoning of others.
4. Model with mathematics.
5. Use appropriate tools strategically.
6. Attend to precision.
7. Look for and make use of structure.
8. Look for and express regularity in repeated reasoning.

\*Gray text indicates Mathematical Practices that are not addressed in this task.

Students' responses to a mathematical task provide evidence of what they understand and are able to do in relation to the standards and practices. Across tasks, this cumulative evidence shows students' understanding and abilities within a domain. When students do not respond completely to all parts of a task, they provide insufficient evidence of their mathematical understanding and abilities and therefore do not fully demonstrate the expectations of the standards and practices aligned with that task.

# A-1a

## Task 1. Multiplication Task

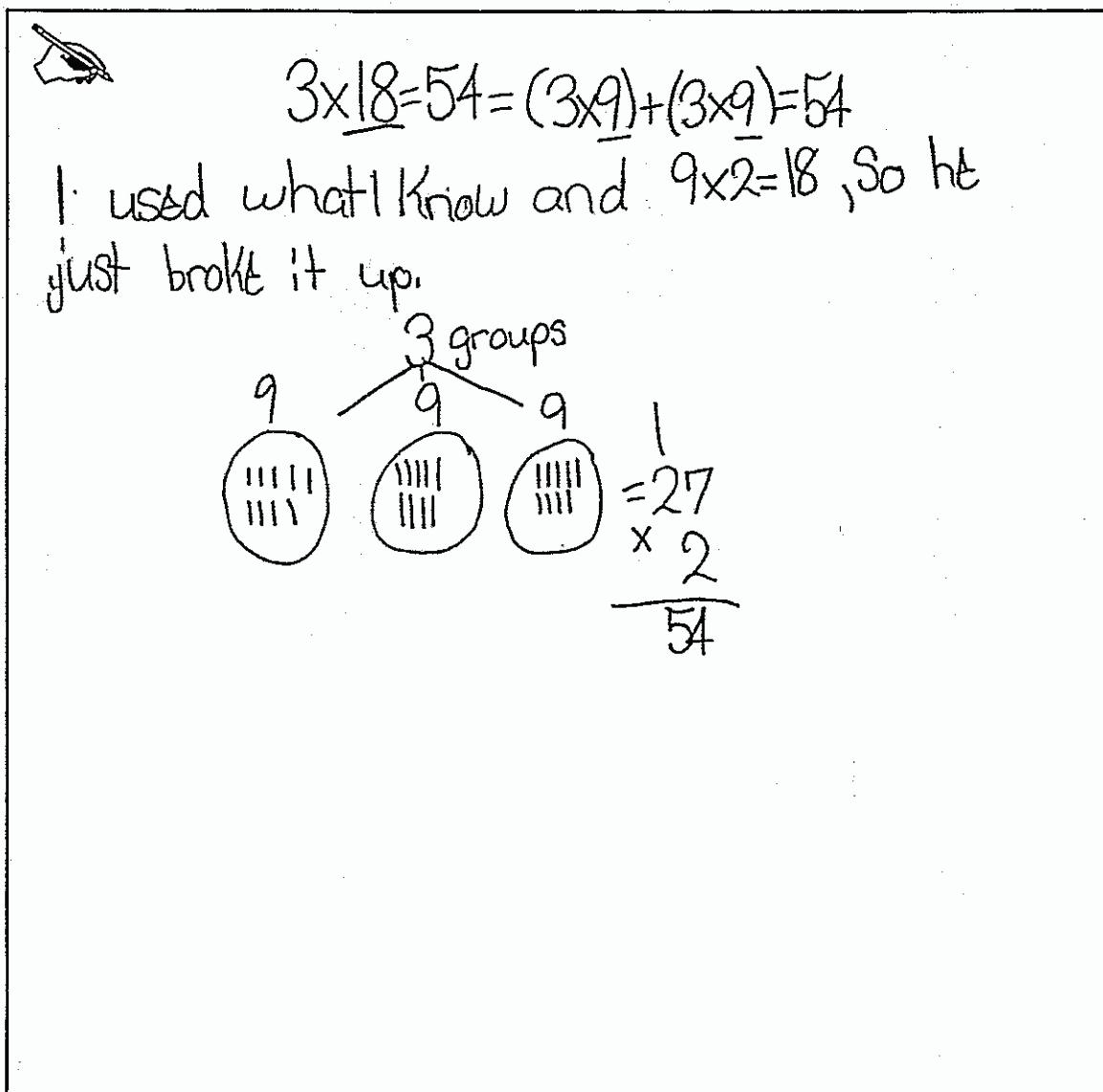
Dylan had to solve this multiplication problem:

$$3 \times 18 = ?$$

Dylan claims, "I can add two multiplication facts I know in order to figure out the product of  $3 \times 18$ . Here is my new expression."

$$(3 \times 9) + (3 \times 9)$$

- a. Draw a diagram of either the multiplication problem,  $3 \times 18$ , or of Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .



# A-1b

- b. Explain the relationship between the multiplication problem,  $3 \times 18$ , and Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .



Dylan's problem was easier that way he wrote it, because he was wanting to break it up.

- c. Use Dylan's method to solve the multiplication problem  $7 \times 19$ . Use a diagram or equation to show the relationship between your new expression and  $7 \times 19$ .



$$(7 \times 10) + (7 \times 9)$$

$$70 + 63 = 133$$

$$\begin{array}{r} 6 \\ 19 \\ \times 7 \\ \hline 133 \end{array}$$

I just added what got from  
 $7 \times 10$  and  $7 \times 9$  and got 133.

Anchor 1

Litho 349995

Total Content Points: 2

(3.OA.A.1, 3.OA.B.5)

Total Practice Points: 2

(MP3, MP4)

In Part A, the student's drawing correctly represents Dylan's expression by showing 3 groups of 9 objects and showing that the product (27) should be multiplied by 2, indicating an understanding of multiplication as representing the number of objects in  $x$  equal groups (3.OA.A.1). The student communicates the relationship between  $(3 \times 9) + (3 \times 9)$  and  $3 \times 18$  by indicating that the products are equal (" $3 \times 18 = 54 = (3 \times 9) + (3 \times 9) = 54$ ") and that the factor 9 is used twice to equal the 18 in  $3 \times 18$  ("9  $\times$  2 = 18, so he just broke it up") (MP3). Either explanation would communicate the relationship. In Part C, the student correctly partitions  $7 \times 19$  into  $(7 \times 10) + (7 \times 9)$  and indicates that both expressions have the same product (133), thereby applying the distributive property of multiplication (3.OA.B.5). The equations in Part A ( $3 \times 18 = 54 = (3 \times 9) + (3 \times 9) = 54$ ) and Part C ( $19 \times 7 = 133$ ) correctly model the solutions for  $3 \times 18$ ,  $(3 \times 9) + (3 \times 9)$ , and  $7 \times 19$  (MP4).

Total Awarded Points: 4 out of 4

**Task 1. Multiplication Task**

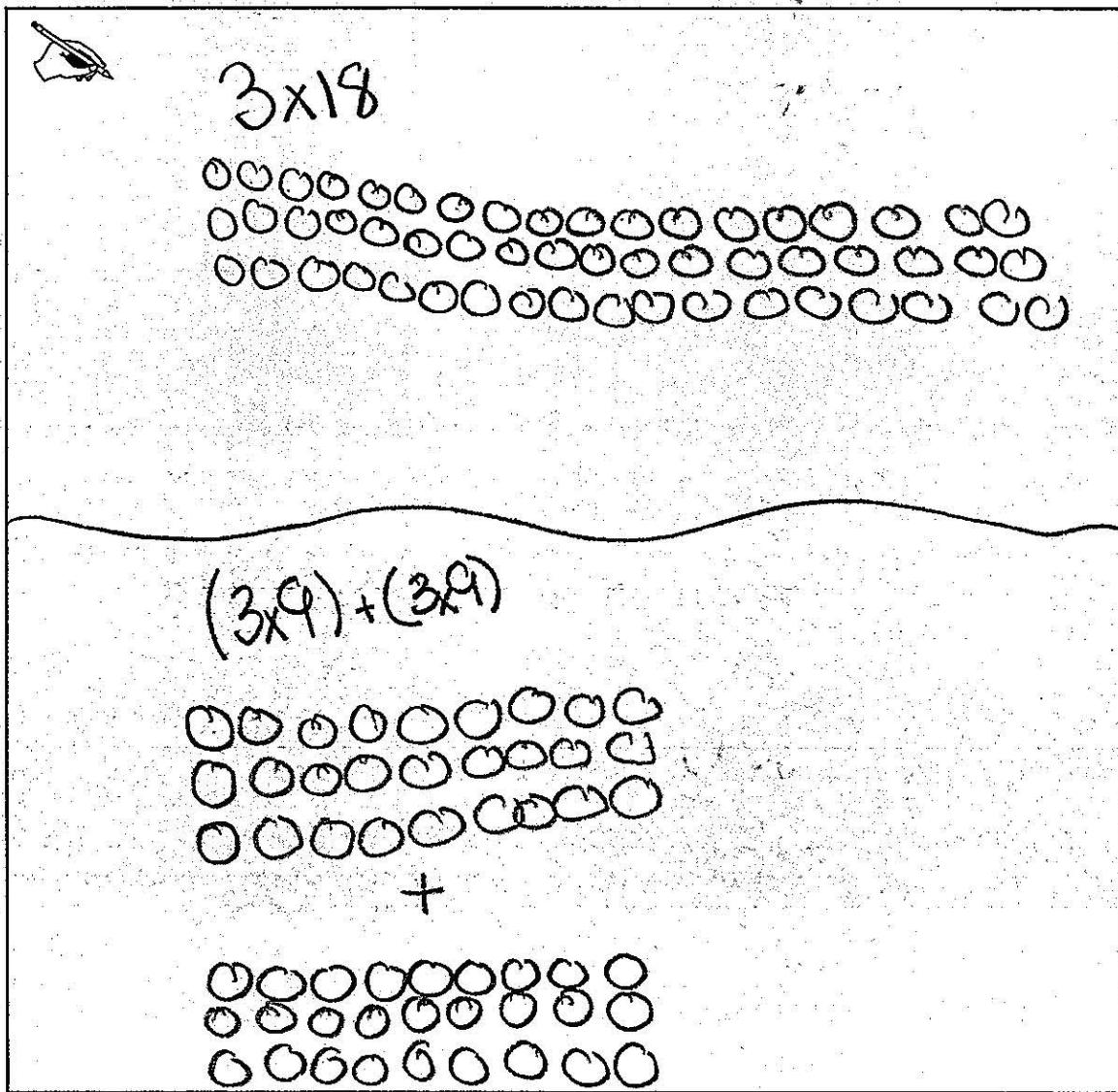
Dylan had to solve this multiplication problem:

$$3 \times 18 = ?$$

Dylan claims, "I can add two multiplication facts I know in order to figure out the product of  $3 \times 18$ . Here is my new expression."

$$(3 \times 9) + (3 \times 9)$$

- a. Draw a diagram of either the multiplication problem,  $3 \times 18$ , or of Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .



# A-2b

- b. Explain the relationship between the multiplication problem,  $3 \times 18$ , and Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .



They are equal + they are because  
 $9+9=18$  so, if  $9+9=18$  then you  
can do  $3 \times 9$  twice. When you  
multiply  $3 \times 18$  you get the same  
as when you add the product  
of  $3 \times 9$  twice, because  $(3 \times 9) + (3 \times 9)$   
is just  $3 \times 18$  broken down so  
Dylan will be able to do  
this problem.

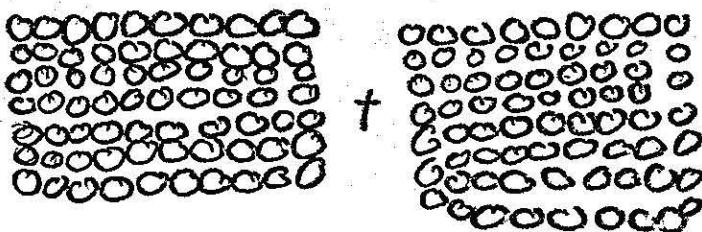
- c. Use Dylan's method to solve the multiplication problem  $7 \times 19$ . Use a diagram or equation to show the relationship between your new expression and  $7 \times 19$ .



$$7 \times 19 = 133$$



$$(7 \times 10) + (7 \times 9)$$



Anchor 2

Litho 363880

Total Content Points: 2

(3.OA.A.1, 3.OA.B.5)

Total Practice Points: 2

(MP3, MP4)

In Part A, the student's drawing correctly represents  $3 \times 18$  by showing 3 groups of 18 objects, indicating an understanding of multiplication as representing the number of objects in  $x$  equal groups (3.OA.A.1). In Part B, the student communicates the relationship between  $(3 \times 9) + (3 \times 9)$  and  $3 \times 18$  by stating that the products are equal and that the factors 9 + 9 equal the 18 in  $3 \times 18$  (MP3). In Part C, the student correctly partitions  $7 \times 19$  into  $(7 \times 10) + (7 \times 9)$  in the diagram and represents that both  $7 \times 19$  and  $(7 \times 10) + (7 \times 9)$  have the same product (133), thereby applying the distributive property of multiplication (3.OA.B.5). The diagrams in Parts A and C correctly model the solutions for  $3 \times 18$ ,  $(3 \times 9) + (3 \times 9)$ ,  $7 \times 19$ , and  $(7 \times 10) + (7 \times 9)$  (MP4).

Total Awarded Points: 4 out of 4

# A-3a

## Task 1. Multiplication Task

Dylan had to solve this multiplication problem:

$$3 \times 18 = ?$$

Dylan claims, "I can add two multiplication facts I know in order to figure out the product of  $3 \times 18$ . Here is my new expression."

---

$$(3 \times 9) + (3 \times 9)$$

- a. Draw a diagram of either the multiplication problem,  $3 \times 18$ , or of Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .

The diagram shows a handwritten addition problem. On the left, there is a drawing of a hand holding a pencil. Below it, there are two groups of circles representing tens and ones. The first group has 3 tens (each ten is a cluster of 10 circles) and 9 ones (9 individual circles). The second group also has 3 tens and 9 ones. A plus sign (+) is placed between the two groups, and a horizontal line extends from the right side of the second group to the right edge of the page.

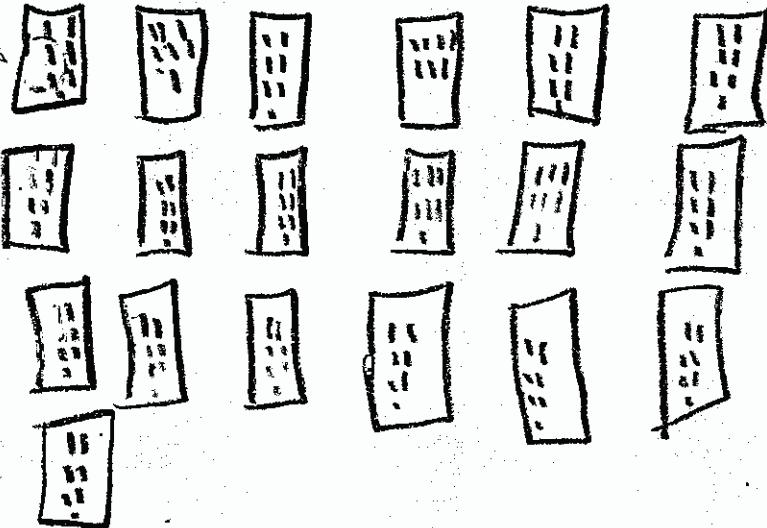
# A-3b

- b. Explain the relationship between the multiplication problem,  $3 \times 18$ , and Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .

  $3 \times 18 = 54$  and  $(3 \times 9) + (3 \times 9) = 54$ , they equal the same.

- c. Use Dylan's method to solve the multiplication problem  $7 \times 19$ . Use a diagram or equation to show the relationship between your new expression and  $7 \times 19$ .





Anchor 3

Litho 365677

Total Content Points: 1 (3.OA.A.1)

Total Practice Points: 2 (MP3, MP4)

In Part A, the student's drawing correctly represents  $(3 \times 9) + (3 \times 9)$  by showing 3 groups of 9 items twice, indicating an understanding of multiplication as representing the number of objects in  $x$  equal groups (3.OA.A.1). In Part B, the student communicates the relationship between  $(3 \times 9) + (3 \times 9)$  and  $3 \times 18$  by stating that the products are equal (" $3 \times 18 = 54$  and  $(3 \times 9) + (3 \times 9) = 54$ ") (MP3). In Part C, the student does not partition one or both factors of  $7 \times 19$ , and therefore does not apply the distributive property of multiplication (no credit for 3.OA.B.5). The diagrams in Parts A, B, and C correctly model the solutions for  $(3 \times 9) + (3 \times 9)$ ,  $3 \times 18$ , and  $7 \times 19$  (MP4).

Total Awarded Points: 3 out of 4

# A-4a

## Task 1. Multiplication Task

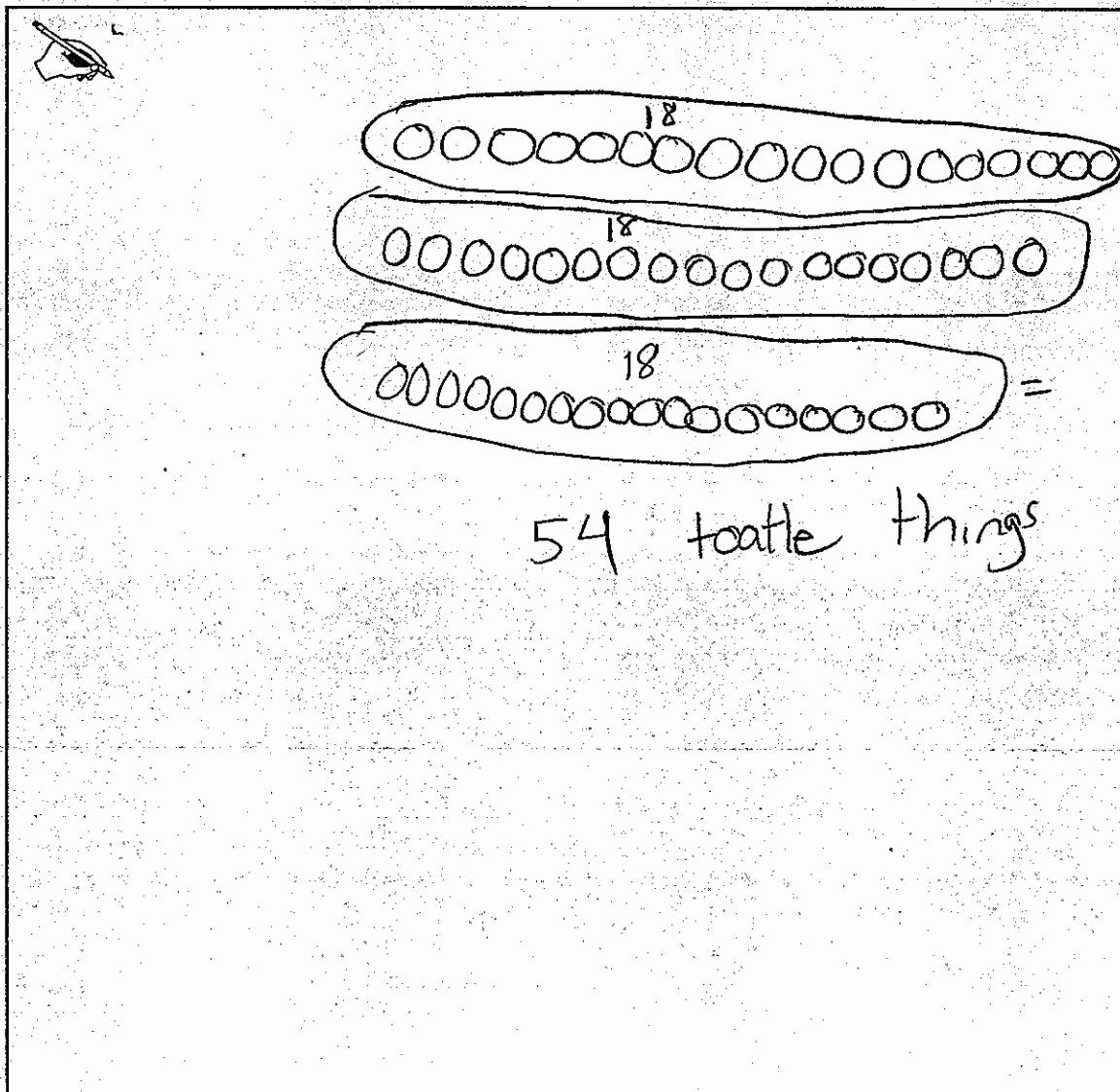
Dylan had to solve this multiplication problem:

$$3 \times 18 = ?$$

Dylan claims, "I can add two multiplication facts I know in order to figure out the product of  $3 \times 18$ . Here is my new expression."

$$(3 \times 9) + (3 \times 9)$$

- a. Draw a diagram of either the multiplication problem,  $3 \times 18$ , or of Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .



# A-4b

- b. Explain the relationship between the multiplication problem,  $3 \times 18$ , and Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .



They Both equal 54

Because 18 3 times =

54 and  $3 \times 9 = 27$  if you put it together which

the other  $3 \times 9$  you will get

54.

- c. Use Dylan's method to solve the multiplication problem  $7 \times 19$ . Use a diagram or equation to show the relationship between your new expression and  $7 \times 19$ .



$$7 \times 19 = 133$$

New expression

$$(3 \times 9) + (3 \times 9) =$$

54

They are different

Because  $7 \times 19 = 133$  The  
New expression is 54

Anchor 4

Litho 363865

Total Content Points: 1 (3.OA.A.1)

Total Practice Points: 2 (MP3, MP4)

In Part A, the student's drawing correctly represents  $3 \times 18$  by showing 3 groups of 18 objects, indicating an understanding of multiplication as representing the number of objects in  $x$  equal groups (3.OA.A.1). In Part B, the student communicates the relationship between  $(3 \times 9) + (3 \times 9)$  and  $3 \times 18$  by stating that the products are equal ("They both equal 54") (MP3). In Part C, the student does not partition one or both factors of  $7 \times 19$ , and therefore does not apply the distributive property of multiplication (no credit for 3.OA.B.5). The drawing in Part A and the equations in Part C correctly model the solutions for  $7 \times 19$  and  $(3 \times 9) + (3 \times 9)$  (MP4).

Total Awarded Points: 3 out of 4

## Task 1. Multiplication Task

Dylan had to solve this multiplication problem:

$$3 \times 18 = ?$$

Dylan claims, "I can add two multiplication facts I know in order to figure out the product of  $3 \times 18$ . Here is my new expression."

$$(3 \times 9) + (3 \times 9)$$

- a. Draw a diagram of either the multiplication problem,  $3 \times 18$ , or of Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .

Handwritten calculations inside the box:

$(3 \times 9) + (3 \times 9) = 54$

$3 \times 11 = 33$

# A-5b

- b. Explain the relationship between the multiplication problem,  $3 \times 18$ , and Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .



$$3 \times 18 = 54 \text{ and } 18$$

$$(3 \times 9) + (3 \times 9) = 54 \text{ also } 50$$

they are the same,

- c. Use Dylan's method to solve the multiplication problem  $7 \times 19$ . Use a diagram or equation to show the relationship between your new expression and  $7 \times 19$ .



$$7 \times 19 = 133$$

$$(7 \times 10) + (7 \times 9) = 133$$

Anchor 5

Litho 368019

Total Content Points: 1 (3.OA.B.5)

Total Practice Points: 2 (MP3, MP4)

In Part A, the student provides no drawing and no explanation of objects in equal groups, and therefore does not indicate an understanding of multiplication as representing the number of objects in  $x$  equal groups (no credit for 3.OA.A.1). In Part B, the student communicates the relationship between  $(3 \times 9) + (3 \times 9)$  and  $3 \times 18$  by stating that the products are equal (“ $3 \times 18 = 54$  and  $(3 \times 9) + (3 \times 9) = 54$  also so they are the same”) (MP3). In Part C, the student correctly partitions  $7 \times 19$  into  $(7 \times 10) + (7 \times 9)$  and indicates that both expressions have the same product (133), thereby applying the distributive property of multiplication (3.OA.B.5). The equations in Parts A, B, and C correctly model the solutions for  $(3 \times 9) + (3 \times 9)$ ,  $3 \times 18$ ,  $7 \times 19$ , and  $(7 \times 10) + (7 \times 9)$  (MP4).

Total Awarded Points: 3 out of 4

**Task 1. Multiplication Task**

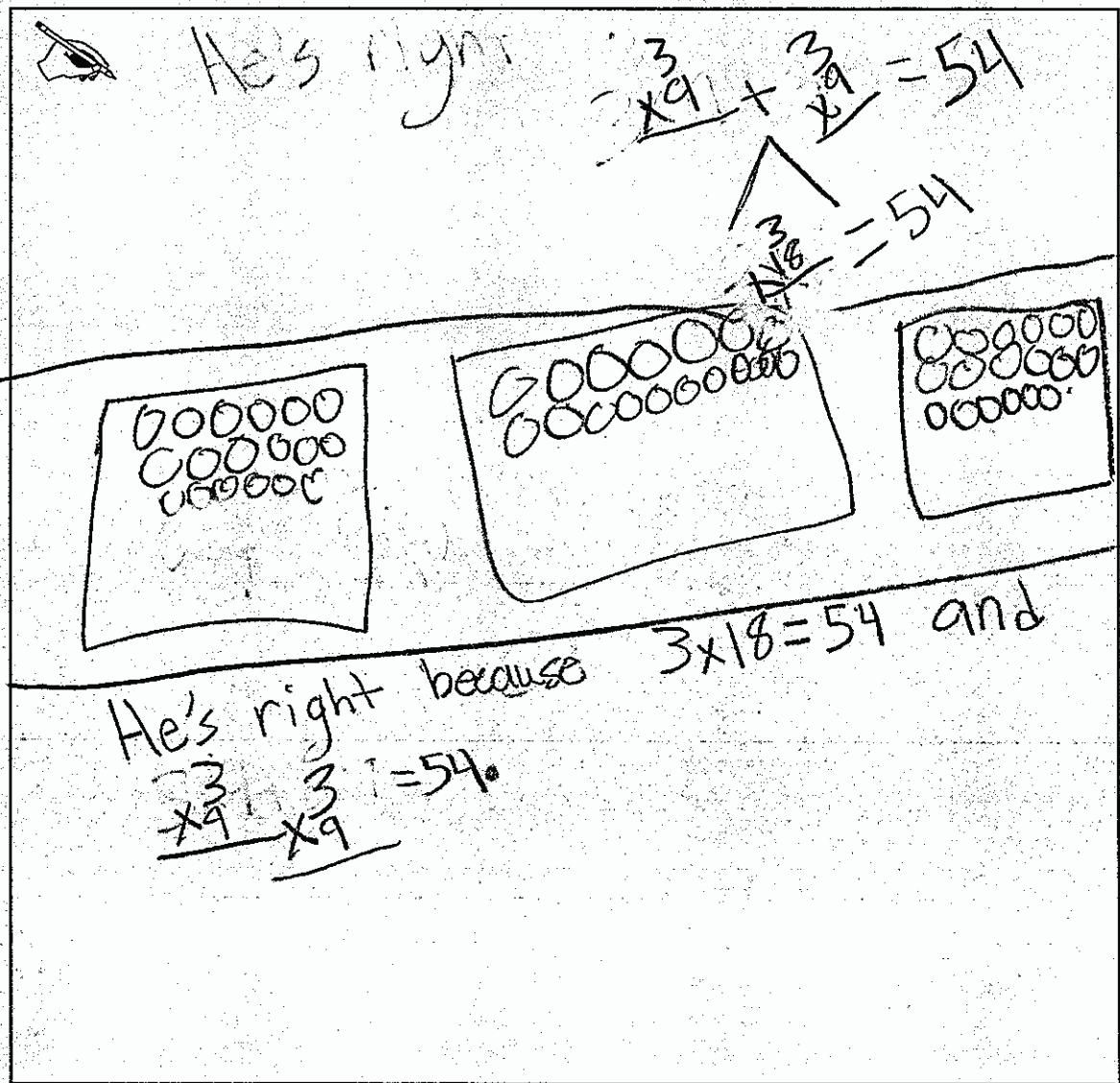
Dylan had to solve this multiplication problem:

$$3 \times 18 = ?$$

Dylan claims, "I can add two multiplication facts I know in order to figure out the product of  $3 \times 18$ . Here is my new expression."

$$(3 \times 9) + (3 \times 9)$$

- a. Draw a diagram of either the multiplication problem,  $3 \times 18$ , or of Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .



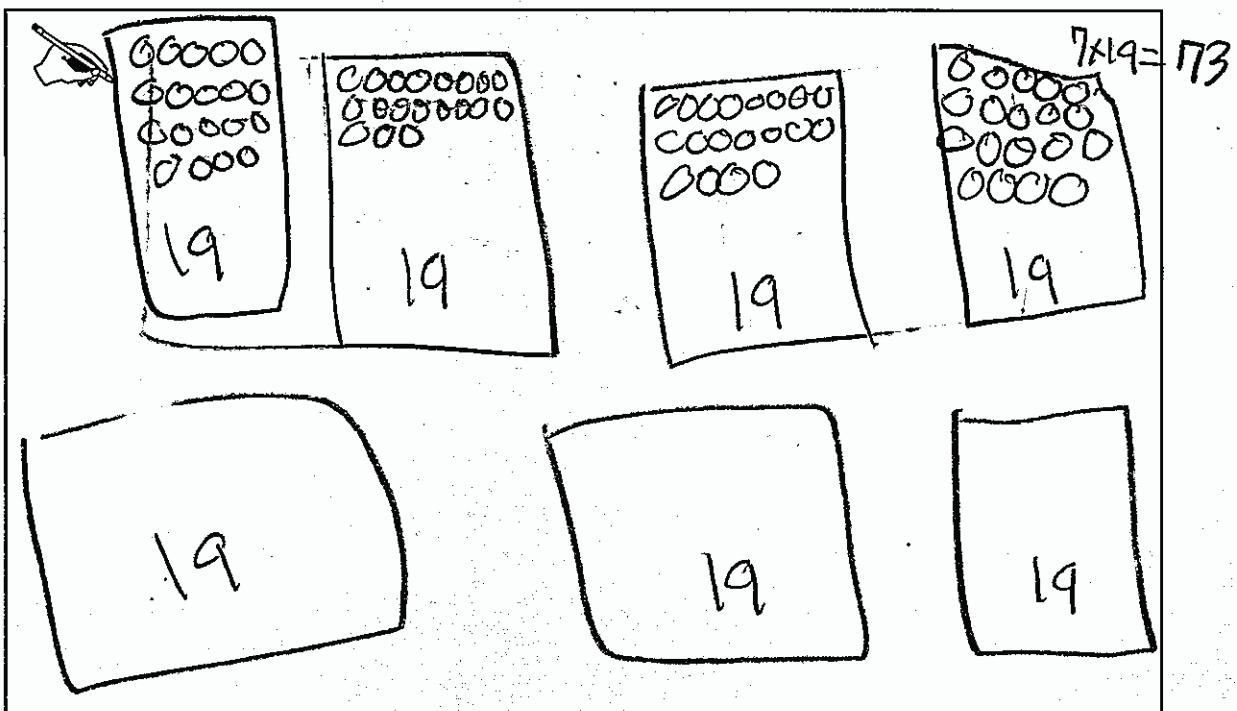
# A-6b

- b. Explain the relationship between the multiplication problem,  $3 \times 18$ , and Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .

 Well  $9+9=18$  so in  
 $3 \times 9 + 3 \times 9$   
 $\swarrow$   
 $9+9=18$   
 $\uparrow$   
 $3 \times 9$

- c. Use Dylan's method to solve the multiplication problem  $7 \times 19$ . Use a diagram or equation to show the relationship between your new expression and  $7 \times 19$ .

  $7 \times 19 = 133$



Anchor 6

Litho 366052

Total Content Points: 1 (3.OA.A.1)

Total Practice Points: 1 (MP3)

In Part A, the student's drawing correctly represents  $3 \times 18$  by showing 3 groups of 18 objects, indicating an understanding of multiplication as representing the number of objects in  $x$  equal groups (3.OA.A.1). In Part B, the student communicates the relationship between  $(3 \times 9) + (3 \times 9)$  and  $3 \times 18$  by indicating that  $9 + 9 = 18$  in  $3 \times 18$  (MP3). In Part C, the student does not partition one or both factors of  $7 \times 19$ , and therefore does not apply the distributive property of multiplication (no credit for 3.OA.B.5). Although the drawing and equations in Part A correctly model the solutions for  $3 \times 18$  and  $(3 \times 9) + (3 \times 9)$ , the equation in Part C is incorrect ( $7 \times 19 = 73$ ), and the diagram is not a correct model for solving  $7 \times 19$  (no credit for MP4).

Total Awarded Points: 2 out of 4

**Task 1. Multiplication Task**

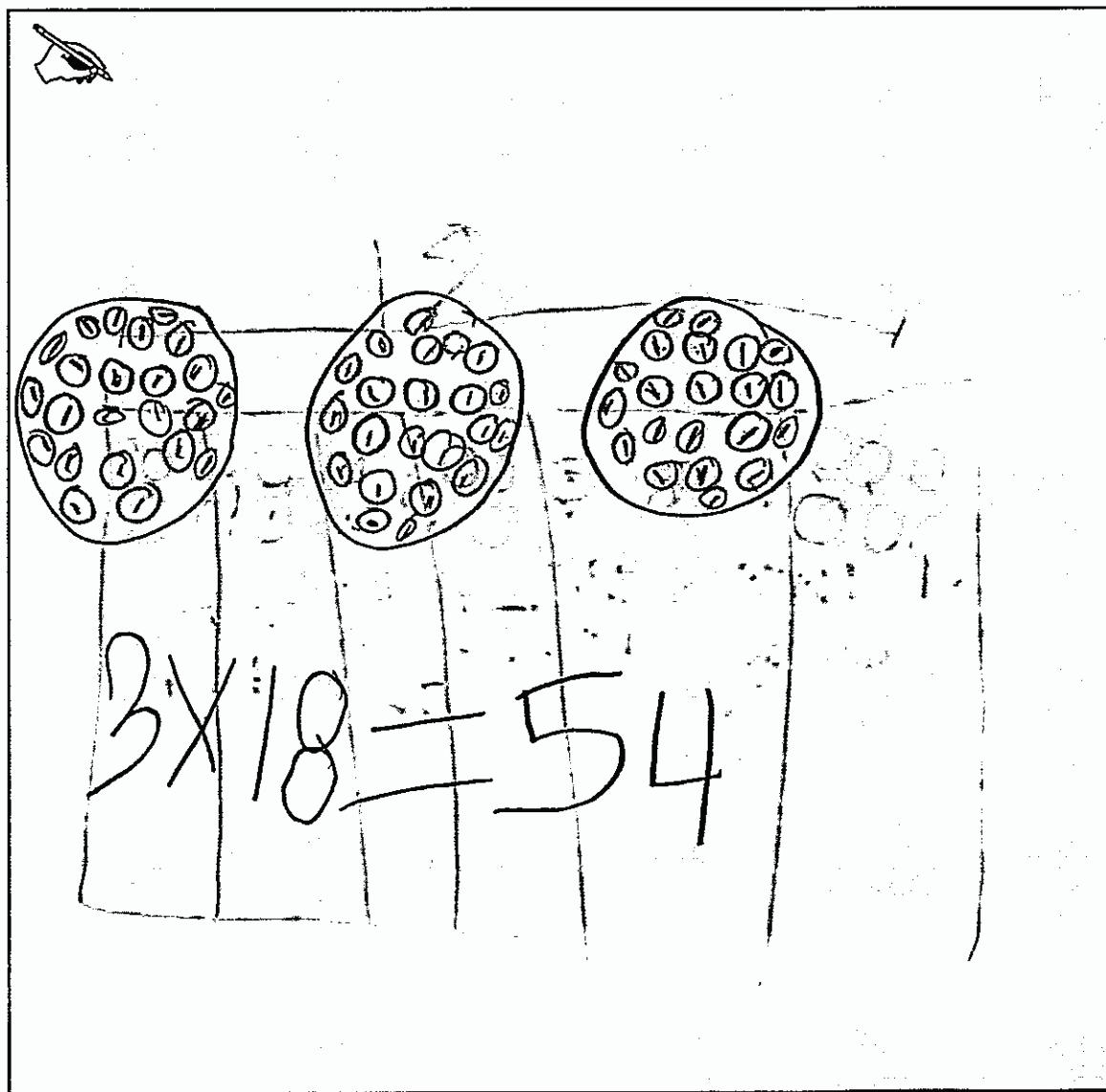
Dylan had to solve this multiplication problem:

$$3 \times 18 = ?$$

Dylan claims, "I can add two multiplication facts I know in order to figure out the product of  $3 \times 18$ . Here is my new expression."

$$(3 \times 9) + (3 \times 9)$$

- a. Draw a diagram of either the multiplication problem,  $3 \times 18$ , or of Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .



# A-7b

- b. Explain the relationship between the multiplication problem,  $3 \times 18$ , and Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .

  $3 \times 18 = 54$  and  $(3 \times 9) + (3 \times 9) = 54$   
so both of them = the  
same  $3 \times 9 = 27$  and  $27 + 27 = 54$   
so they are the same

- c. Use Dylan's method to solve the multiplication problem  $7 \times 19$ . Use a diagram or equation to show the relationship between your new expression and  $7 \times 19$ .

  $7 \times 19 = 133$  is the same  
as  $(67 + 67) - 1 = 133$  because if  
I just do  $67 + 67$  it will = 134 but if  
I - 1 it will = 133.

Anchor 7

Litho 364507

Total Content Points: 1 (3.OA.A.1)

Total Practice Points: 1 (MP3)

In Part A, the student's drawing correctly represents  $3 \times 18$  by showing 3 groups of 18 objects, indicating an understanding of multiplication as representing the number of objects in  $x$  equal groups (3.OA.A.1). In Part B, the student communicates the relationship between  $(3 \times 9) + (3 \times 9)$  and  $3 \times 18$  by stating that the products are equal (" $3 \times 18 = 54$  and  $(3 \times 9) + (3 \times 9) = 54$ ") (MP3). The inaccurate equations in Part B (" $3 \times 9 = 37$  and  $37 + 37 = 54$ ") are not correct models for solving Dylan's expression (no credit for MP4). In Part C, the student does not correctly partition one or both factors of  $7 \times 19$  ( $67 + 67 - 1$ ), and therefore does not apply the distributive property of multiplication (no credit for 3.OA.B.5).

Total Awarded Points: 2 out of 4

# A-8a

## Task 1. Multiplication Task

Dylan had to solve this multiplication problem:

$$3 \times 18 = ?$$

Dylan claims, "I can add two multiplication facts I know in order to figure out the product of  $3 \times 18$ . Here is my new expression."

$$(3 \times 9) + (3 \times 9)$$

- a. Draw a diagram of either the multiplication problem,  $3 \times 18$ , or of Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .

$\underline{(3 \times 9) + (3 \times 9) = 54}$  He is right +  $\underline{3 \times 18 = 54}$

# A-8b

- b. Explain the relationship between the multiplication problem,  $3 \times 18$ , and Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .

  $3 \times 18 = 54$  He did the other  
problem and solved the answer  
 $(3 \times 4) + (3 \times 4) = 54$

- c. Use Dylan's method to solve the multiplication problem  $7 \times 19$ . Use a diagram or equation to show the relationship between your new expression and  $7 \times 19$ .

 He got  $7 \times 19 = 133$  He is  
Correct.  $19 \times 7 = 133$

Anchor 8

Litho 372747

Total Content Points: 0

Total Practice Points: 2 (MP3, MP4)

In Part A, the student provides no drawing and no explanation of objects in equal groups, and therefore does not indicate an understanding of multiplication as representing the number of objects in  $x$  equal groups (no credit for 3.OA.A.1). In Parts A and B, the student communicates the relationship between  $(3 \times 9) + (3 \times 9)$  and  $3 \times 18$  by showing that both expressions have the same product, 54 (MP3). In Part C, the student does not partition one or both factors of  $7 \times 19$ , and therefore does not apply the distributive property of multiplication (no credit for 3.OA.B.5). The equations in Parts A, B, and C correctly model the solutions for  $3 \times 18$ ,  $(3 \times 9) + (3 \times 9)$ , and  $7 \times 19$  (MP4).

Total Awarded Points: 2 out of 4

# A-9a

## Task 1. Multiplication Task

Dylan had to solve this multiplication problem:

$$3 \times 18 = ?$$

Dylan claims, "I can add two multiplication facts I know in order to figure out the product of  $3 \times 18$ . Here is my new expression."

$$(3 \times 9) + (3 \times 9)$$

- a. Draw a diagram of either the multiplication problem,  $3 \times 18$ , or of Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .

The diagram consists of a rectangular box containing handwritten text. In the top-left corner of the box, there is a small drawing of a hand holding a pencil. Below this, the multiplication problem  $3 \times 18 = 54$  is written in large, bold letters. Underneath the equation, the text "is the one" is written, followed by "he needs to" and "because".

# A-9b

- b. Explain the relationship between the multiplication problem,  $3 \times 18$ , and Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .



He could use his expression

but it would be easier to  $3 \times 18 = 54$

because he wouldn't get the right answer

- c. Use Dylan's method to solve the multiplication problem  $7 \times 19$ . Use a diagram or equation to show the relationship between your new expression and  $7 \times 19$ .



$$7 \times 1\cancel{9} = 106$$

$$7 \times 19 = 106$$

$$10 \times 7 = 70$$

$$\begin{array}{r} 9 \times 7 = 30 \\ \hline 106 \end{array}$$

Anchor 9

Litho 362013

Total Content Points: 1 (3.OA.B.5)

Total Practice Points: 0

The student provides no drawing and no explanation of objects in equal groups, and therefore does not indicate an understanding of multiplication as representing the number of objects in  $x$  equal groups (no credit for 3.OA.A.1). In Part B, the student's response ("He could use his [expression] but it would be [easier] to  $3 \times 18 = 54$  because he wouldn't get the right answer") does not correctly communicate the relationship between  $(3 \times 9) + (3 \times 9)$  and  $3 \times 18$  (no credit for MP3). In Part C, although the multiplication is incorrect, the student correctly partitions  $7 \times 19$  into  $(10 \times 7) + (9 \times 7)$  and indicates that both have the same product of 106, thereby applying the distributive property of multiplication (3.OA.B.5). However, the inaccurate equation in Part C ( $7 \times 19 = 106$ ) is not a correct model for solving  $7 \times 19$  (no credit for MP4).

Total Awarded Points: 1 out of 4

# A-10a

## Task 1. Multiplication Task

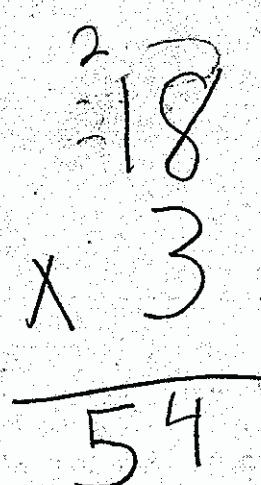
Dylan had to solve this multiplication problem:

$$3 \times 18 = ?$$

Dylan claims, "I can add two multiplication facts I know in order to figure out the product of  $3 \times 18$ . Here is my new expression."

$$(3 \times 9) + (3 \times 9)$$

- a. Draw a diagram of either the multiplication problem,  $3 \times 18$ , or of Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .



A handwritten multiplication problem is shown within a rectangular frame. In the top left corner of the frame, there is a small drawing of a hand holding a pencil. The multiplication problem itself consists of three parts: the first part is the number 218, the second part is a multiplication sign (x), and the third part is the number 3. A horizontal line is drawn below the 3, and the result 54 is written directly beneath it.

# A-10b

- b. Explain the relationship between the multiplication problem,  $3 \times 18$ , and Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .

 Well you have this problem  $\begin{array}{r} 18 \\ \times 3 \\ \hline 24 \end{array}$  if you said  
 $\begin{array}{r} 8 \\ \times 3 \\ \hline 24 \end{array}$ , but on the 2 you have  $\overset{1}{\cancel{8}}$  to carry it to  
the 1 (above)  $\begin{array}{r} & 1 \\ & \downarrow \\ \times & 3 \\ \hline 24 \end{array}$   
 $\cancel{2} + 2 = 5$   
 is your answer

- c. Use Dylan's method to solve the multiplication problem  $7 \times 19$ . Use a diagram or equation to show the relationship between your new expression and  $7 \times 19$ .

  $\begin{array}{r} 6 \ 1 \ 9 \\ \times 7 \\ \hline 423 \end{array}$

Anchor 10

Litho 368083

Total Content Points: 0

Total Practice Points: 1 (MP4)

The student provides no drawings and no explanation of objects in equal groups, and therefore does not indicate an understanding of multiplication as representing the number of objects in  $x$  equal groups (no credit for 3.OA.A.1). In Part B, the student's response does not correctly communicate the relationship between  $(3 \times 9) + (3 \times 9)$  and  $3 \times 18$  (no credit for MP3). In Part C, the student does not partition one or both factors of  $7 \times 19$ , and therefore does not apply the distributive property of multiplication (no credit for 3.OA.B.5). The equations in Parts A, B, and C correctly model the solutions for  $18 \times 3$  and  $19 \times 7$  (MP4).

Total Awarded Points: 1 out of 4

## Task 1. Multiplication Task

Dylan had to solve this multiplication problem:

$$3 \times 18 = ?$$

Dylan claims, "I can add two multiplication facts I know in order to figure out the product of  $3 \times 18$ . Here is my new expression."

$$(3 \times 9) + (3 \times 9)$$

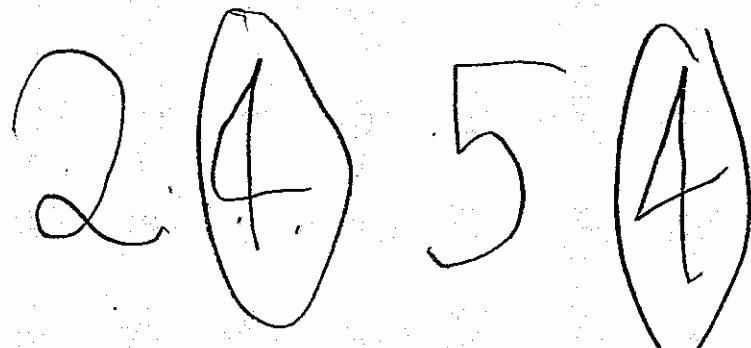
- a. Draw a diagram of either the multiplication problem,  $3 \times 18$ , or of Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .

The image shows handwritten student work on a lined page. At the top left is a small drawing of a hand holding a pencil. To the right of the hand is the equation  $(3 \times 9) + (3 \times 9) =$ . Below this, the word "or" is written. Further down, the equation  $3 \times 18 = 24$  is written. A horizontal line separates this section from the one below. In the lower section, the equation  $(3 \times 9) + (3 \times 9) = 54$  is written, followed by another  $3 \times 18 = 24$ .

# A-11b

- b. Explain the relationship between the multiplication problem,  $3 \times 18$ , and Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .

 one may have 5④ but the other one has  
2④ they have the four in common.



The student has written the number 2050. The tens column (0 and 5) is circled twice, once with a red circle and once with a blue circle, indicating they have two groups of ten in common.

- c. Use Dylan's method to solve the multiplication problem  $7 \times 19$ . Use a diagram or equation to show the relationship between your new expression and  $7 \times 19$ .

  $7 \times 19 = 133$   $133 \div 1 = 133$

---

they both have 33 in them.

Total Content Points: 0

Total Practice Points: 0

The student provides no drawings and no explanation of objects in equal groups, and therefore does not indicate an understanding of multiplication as representing the number of objects in  $x$  equal groups (no credit for 3.OA.A.1). In Part B, the student's response does not correctly communicate the relationship between  $(3 \times 9) + (3 \times 9)$  and  $3 \times 18$  (no credit for MP3). In Part C, the student does not partition one or both factors of  $7 \times 19$ , and therefore does not apply the distributive property of multiplication (no credit for 3.OA.B.5). Although one equation in Part A ( $(3 \times 9) + (3 \times 9) = 54$ ) and the equation in Part C ( $7 \times 19 = 133$ ) are correct models, the inaccurate equation in Part A ( $3 \times 18 = 24$ ) is not a correct model for solving  $3 \times 18$  (no credit for MP4).

Total Awarded Points: 0 out of 4

# A-12a

## Task 1. Multiplication Task

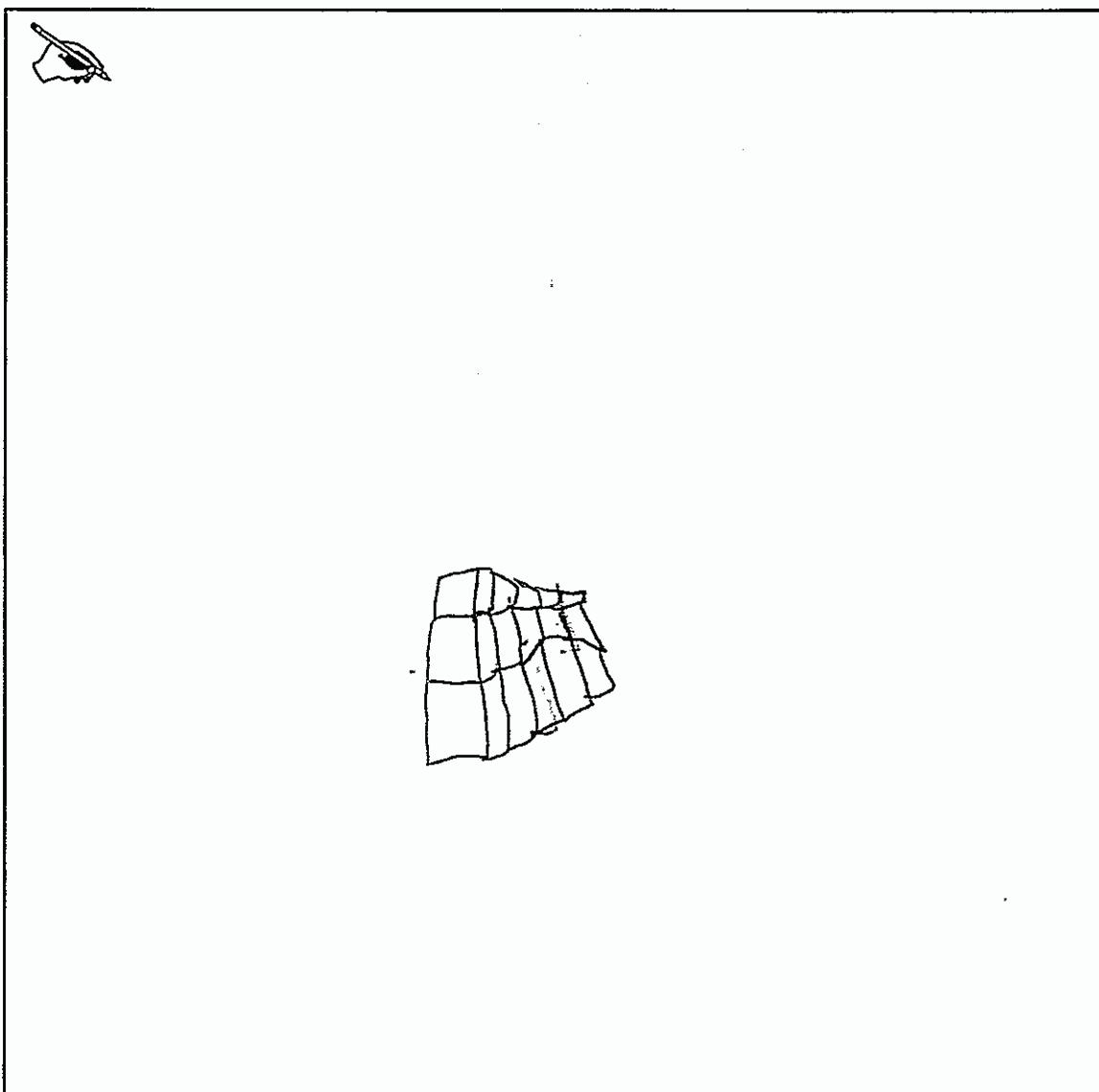
Dylan had to solve this multiplication problem:

$$3 \times 18 = ?$$

Dylan claims, "I can add two multiplication facts I know in order to figure out the product of  $3 \times 18$ . Here is my new expression."

$$(3 \times 9) + (3 \times 9)$$

- a. Draw a diagram of either the multiplication problem,  $3 \times 18$ , or of Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .



# A-12b

- b. Explain the relationship between the multiplication problem,  $3 \times 18$ , and Dylan's expression,  $(3 \times 9) + (3 \times 9)$ .

 They have 3 objects.

$(3 \times 9) + (3 \times 9) = 3 \times 18$

- c. Use Dylan's method to solve the multiplication problem  $7 \times 19$ . Use a diagram or equation to show the relationship between your new expression and  $7 \times 19$ .

  $(3 \times 9) + (3 \times 9) \text{ and } 7 \times 19$

$7 \times 19 = 133$

$$\begin{array}{r} 7 \\ \times 19 \\ \hline 133 \end{array}$$

Anchor 12

Litho 382094

Total Content Points: 0

Total Practice Points: 0

In Part A, the student's drawing does not correctly represent  $3 \times 18$  or  $(3 \times 9) + (3 \times 9)$ , and therefore does not indicate an understanding of multiplication as representing the number of objects in  $x$  equal groups (no credit for 3.OA.A.1). In Part B, the student rewrites the expressions from the prompt but does not communicate the relationship between  $(3 \times 9) + (3 \times 9)$  and  $3 \times 18$  (no credit for MP3). In Part C, the student does not partition one or both factors of  $7 \times 19$ , and therefore does not apply the distributive property of multiplication (no credit for 3.OA.B.5). Although the equation in Part C ( $7 \times 19 = 133$ ) is a correct model for solving  $7 \times 19$ , the student does not provide a model for solving  $(3 \times 9) + (3 \times 9)$  or  $3 \times 18$  (no credit for MP4).

Total Awarded Points: 0 out of 4