# **TNCore**

Task: Car Lot	6 <sup>th</sup> Grade
The local car lot has 8 cars and 5 trucks. The owners are going to buy enough cars and enough trucks to	make the ratio of cars to trucks 3:2.
A) How many cars and how many trucks should the owners buy?	
B) Is there more than one way to buy enough cars and trucks to make the ratio of cars to trucks 3:2?	
C) Describe any patterns you see in solving this problem.	
Common Core State Standards for Mathematical Content	Common Core State Standards for
	Mathematical Practice
6.RP.A.1. Understand the concept of a ratio and use ratio language to describe a ratio relationship	
between two quantities. For example, "The ratio of wings to beaks in the bird house at the zoo was 2:1,	
because for every 2 wings there was 1 beak." "For every vote candidate A received, candidate C	
received nearly three votes."	
	Mathematical Practices
6.RP.A.3. Use ratio and rate reasoning to solve real-world and mathematical problems, e.g., by	1. Make sense of problems and
reasoning about tables of equivalent ratios, tape diagrams, double number line diagrams, or	persevere in solving them.
a Make tables of equivalent ratios relating quantities with whole number measurements find	2. Reason abstractly and
a. Make tables of equivalent ratios relating quantities with whole number measurements, mu missing values in the tables, and plot the pairs of values on the coordinate plane. Use tables to	quantitatively.
compare ratios	3. Construct viable arguments and
	critique the reasoning of others.
6.EE.A.2. Write, read, and evaluate expressions in which letters stand for numbers.	4. Model with mathematics.
a. Write expressions that record operations with numbers and with letters standing for numbers. For	5. Use appropriate tools strategically.
example, express the calculation "Subtract y from 5" as 5 – y.	6. Attend to precision.
	7. Look for and make use of structure.
6.EE.C.9. Use variables to represent two quantities in a real-world problem that change in relationship	8. LOOK for and express regularity in
to one another; write an equation to express one quantity, thought of as the dependent variable, in	
terms of the other quantity, thought of as the independent variable. Analyze the relationship between	
the dependent and independent variables using graphs and tables, and relate these to the equation.	
For example, in a problem involving motion at constant speed, list and graph ordered pairs of distances	
and times, and write the equation d = 65t to represent the relationship between distance and time.	
Essential Understandings	
<ul> <li>Reasoning with ratios involves attending to and coordinating two quantities.</li> </ul>	
Ratios are often expressed in fraction notation, although ratios and fractions do not have identic	al meaning.
Ratios are often used to make "part-part" comparisons, but fractions are not.	

• Using variables permits representing varying quantities. This use of variables is particularly important in studying relationships between

varying quantities.		
Explore Phase		
Possible Solution Paths	Assessing and Advancing Questions	
	Part A)	
Drawing a Picture	Assessing Questions	
	Why did you choose to group the cars and trucks the way you did?	
A) Students can represent 8 cars and 5 trucks. Since the ratio		
should be 3:2, they can circle groups of 3 cars and 2 trucks.	Advancing Questions	
	Are there other ways to represent the ratio 3:2? How would those other	
	ways be helpful?	
$\begin{pmatrix} C & C & C & T & T \end{pmatrix}$	Part B)	
	Assessing Questions	
	How can you show that there is more than one way to make the ratio of	
	cars to trucks 3:2?	
The third group is missing 1 car and 1 truck, so the owners need to		
purchase 1 additional car and 1 additional truck.	Advancing Questions	
	Are there other ways to represent the ratio 3:2? How would those other	
B) Students can extend the reasoning from part A by including	ways be helpful?	
additional groups of 3 cars and 2 trucks. Additional answers		
include: 4 cars and 3 trucks; 7 cars and 5 trucks; 10 cars and 7	Part C)	
trucks; etc.	Assessing Questions	
	How do you know your pattern is correct?	
C) Patterns: The number of cars purchased should be 1 more than $\frac{1}{2}$		
a multiple of 3 (3x + 1); the corresponding number of trucks should be 1 more than the same multiple of 2 ( $2x + 1$ )	Is there a relationship between the pattern for the number of cars the	
be 1 more than the same multiple of 2 (2x + 1).	owners should buy and the pattern for the number of trucks the owners	
	snould buy?	
	Advancing Questions	
	Advancing Questions	
	is there a pattern to the number of cars the owners should buy? The	
	How can you describe those patterns using a variable?	
	Part A)	
Making a Table	Assessing Questions	
A) Students can represent a table showing ratios equivalent to 3:2	How did you decide how many cars and how many trucks the owners	

to determine the number of cars and trucks the owners need to purchase.

Cars:Trucks =	3:2	
Number of	Number of	Notes
Cars	Trucks	
Needed	Needed	
3	2	The lot already has 8 cars and 5
		trucks—more than these numbers.
6	4	The lot already has 8 cars and 5
		trucks—more than these numbers.
9	6	The lot already has 8 cars and 5
		trucks—the owners can purchase 1
		car and 1 truck.

B) Students can extend the table begun in part A.

Cars:Trucks =	3:2	
Number of	Number of	Notes
Cars	Trucks	
Needed	Needed	
3	2	The lot already has 8 cars and 5
		trucks—more than these numbers.
6	4	The lot already has 8 cars and 5
		trucks—more than these numbers.
9	6	The lot already has 8 cars and 5
		trucks—the owners can purchase 1
		car and 1 truck.
12	8	The lot already has 8 cars and 5
		trucks—the owners can purchase 4
		cars and 3 trucks.
15	10	The lot already has 8 cars and 5
		trucks—the owners can purchase 7
		cars and 2 trucks.
etc.	etc.	

#### should buy?

#### Advancing Questions

Are there other ways to represent the ratio 3:2? How would those other ways be helpful?

## Part B)

#### Assessing Questions

How can you show that there is more than one way to make the ratio of cars to trucks 3:2?

## Advancing Questions

Are there other ways to represent the ratio 3:2? How would those other ways be helpful?

# Part C)

<u>Assessing Questions</u> How do you know your pattern is correct?

What does the variable in your pattern represent?

Is there a relationship between the pattern for the number of cars the owners should buy and the pattern for the number of trucks the owners should buy?

### Advancing Questions

Is there a pattern to the number of cars the owners should buy? The number of trucks?

How can you describe those patterns using a variable?

C) Since the r	number of cars bo	ought increases b	oy 3 at each step, v	ve	
know that the	e pattern should h	nave 3 (a variable	e) in it.  The		
sequence des	cribing the numb	er of cars bough	it is an arithmetic		
sequence tha	t begins with 1, so	o the pattern is 3	3x + 1, where x is a		
whole numbe	er. Similarly, the p	battern for the n	umber of trucks is	2x	
+ 1. It is impo	ortant to note tha	t to find an ansv	ver to problem A, t	he	
same value fo	or x should be use	d in both patter	ns.		
Number of	Pattern for the	Number of	Pattern for the		
Cars Bought	number of cars	Trucks Bought	number of trucks		
1	3 (0) + 1	1	2 (0) + 1		
4	3 (1) + 1	3	2 (1) + 1		
7	3 (2) + 1	5	2 (2) + 1		
10	3 (3) + 1	7	2 (3) + 1		
Possible Stud	ent Misconceptio	ons			
					Assessing Questions
					What does the ratio 3:2 mean in the problem? What is the ratio of cars to
					trucks now?
Students may	not think a solut	ion is possible si	nce 3:2 implies 3 c	ars	
and 2 trucks,	and the car lot all	ready has 8 cars	and 5 trucks.		Advancing Questions
			Are there other ways to write the ratio 3:2? How could these other ways		
			help vou?		
			Assessing Questions		
			What does the ratio 3.2 mean in the problem? What does the 3		
					represent and what does the 2 represent in the ratio?
			represent and what does the 2 represent in the ratio.		
Students may	confuse 3:2 as th	ne ratio of trucks	s to cars.		Advancing Questions
			Are there other ways to write the ratio 3:2? How do you know which		
			number in your ratios represents the number of cars and which		
			represents the number of trucks? How would this help?		
			Accossing Questions		
			Assessing Questions		
Patterns: Students may describe the pattern for the number of cars		ars	Tell me what pattern you see in your answers. How can you describe this		
bought as 3x or as x + 3 rather than 3x + 1. Similar issues arise for		r	patterne		
the pattern for the number of trucks bought.			Whet do no the control is a second to be a second t		
		what does the variable represent in your pattern?			

	Advancing Questions	
	What kinds of numbers can you use in place of the variable in your	
	expression? Do your answers from your expression match the answers	
	you found in part B?	
	How would you decide how many cars the owners should buy if they buy	
	5 trucks? How do you know? What number do you use for x in your	
	expression to determine the number of cars?	
Entry/Extensions	Assessing and Advancing Questions	
	Assessing Questions	
	Let's look at what is already on the car lot. How many cars and how many	
	trucks do you have? What is the ratio of cars to trucks now? Why?	
If students can't get started		
	Advancing Questions	
	How can you change that ratio? What would you need to do to change	
	that ratio?	
	Assessing Questions	
	Show me how you determined the expressions for the patterns you	
	found.	
	What kinds of numbers can you use in your expressions for the variable?	
If students finish souly		
If students finish early	Is the variable in your expression for the number of cars related to the	
	variable in your expression for the number of trucks?	
	Advancing Questions	
	Suppose the ratio of trucks to cars was 3:2. How would this change your	
	answers? Would you have different patterns? Why or why not?	
Discuss/Analyze		
Whole Group Questions		
What strategies did you use to solve this problem? How did you know your strategy would work?		
How are ratios in part B similar to what you know about fractions? How are the ratios different than what you know about fractions?		
What kinds of numbers can you use in your expressions for the variable? Is the variable in your expression for the number of cars related to the		
variable in your expression for the number of trucks?		